

# CONTINGENCY TABLES

## Question 1 (\*\*)

The music preferences of 500 individuals are summarized in the table below.

	Pop	Rock	Dance	Soul
Males	81	42	49	92
Females	110	31	36	59

Use a  $\chi^2$  test, at the 1% level of significance, to investigate whether there is any association between the gender and the preferred music.

☐ , association,  $13.736 > 11.345$

$H_0$  : THERE IS NO ASSOCIATION, BETWEEN GENDER & MUSIC PREFERENCE, i.e. THE CATEGORIES ARE INDEPENDENT.  
 $H_1$  : THERE IS ASSOCIATION BETWEEN GENDER & MUSIC PREFERENCE, i.e. THE CATEGORIES ARE NOT INDEPENDENT.

	POP	ROCK	DANCE	SOUL	TOTAL
MALES	81 3.96	42 3.94	49 0.18	92 1.89	264
FEMALES	110 4.57	31 0.97	36 0.43	59 2.11	236
TOTAL	191	73	85	151	500

$O_i = \text{ACTUAL DATA} - \text{OBSERVED VALUES } O_i$   
 $E_i = \text{EXPECTED (IF INDEPENDENT) } E_i$   
 $\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$

- DEGREES OF FREEDOM  $\rightarrow (C-1)(R-1) = (2-1)(2-1) = 1$
- $\chi^2_{0.01}(1) = 11.345$
- $\sum \frac{(O_i - E_i)^2}{E_i} = 13.736$

As  $13.736 > 11.345$  THERE IS EVIDENCE OF ASSOCIATION BETWEEN GENDER AND THE PREFERRED MUSIC - THERE IS SUFFICIENT EVIDENCE TO REJECT  $H_0$

## Question 2 (\*\*)

A cinema manager believes that there is an association between the gender of his customers and the type of film they come to watch. The table below shows 1000 viewers in this cinema classified by gender and by the type of film they watched.

	Action Film	Comedy Film	Romance Film
Male	239	185	140
Female	155	150	131

Use a  $\chi^2$  test, at the 5% level of significance, to investigate whether there is evidence to support the manager's claim.

$\chi^2 = 5.571$ , no association,  $5.571 < 5.991$

**SETTING HYPOTHESES**

$H_0$ : THERE IS NO ASSOCIATION BETWEEN GENDER & FILM TYPE PREFERENCE, i.e. THE FILMS ARE INDEPENDENT

$H_1$ : THERE IS ASSOCIATION BETWEEN GENDER & FILM PREFERENCE, i.e. THE FILMS ARE NOT INDEPENDENT

**SETTING A MULTIPURPOSE TABLE**

	ACTION FILM	COMEDY FILM	ROMANCE FILM	TOTAL
MALE	239 239/1000 0.239	185 185/1000 0.185	140 140/1000 0.140	564
FEMALE	155 155/1000 0.155	150 150/1000 0.150	131 131/1000 0.131	436
TOTAL	394	335	271	1000

$O$  = ACTUAL DATA = OBSERVED FREQUENCY  $O_i$   
 $E$  = EXPECTED RESPONSE  $E_i$  (if independent)  
 $\chi^2$  = CONTRIBUTIONS  $\sum \frac{(O_i - E_i)^2}{E_i}$

**DETERMINING THE D.F. OF THE STATISTICS**

- degrees of freedom  $D.F. = (r-1)(c-1) = (2-1)(3-1) = 2$
- $\chi^2_{0.05}(2) = 5.991$
- $\sum \frac{(O_i - E_i)^2}{E_i} = 5.571$

As  $5.571 < 5.991$  THERE IS EVIDENCE OF INDEPENDENCE, i.e. IT APPEARS THAT THERE IS NO ASSOCIATION BETWEEN GENDER & TYPE OF FILM — THERE IS NO SUFFICIENT EVIDENCE TO REJECT  $H_0$

## Question 3 (\*\*)

The following table shows a random sample of 200 adults in a Café which ordered tea, coffee or chocolate, classified by gender.

	Tea	Coffee	Chocolate
Male	57	26	11
Female	42	47	17

Use a  $\chi^2$  test, at the 5% level of significance, to investigate whether there is any association between the type of drink ordered and gender.

☐ , association,  $8.912 > 5.991$

$H_0$ : THERE IS NO ASSOCIATION BETWEEN GENDER & CHOICE OF DRINK (EVENTS ARE INDEPENDENT)  
 $H_1$ : THERE IS ASSOCIATION BETWEEN GENDER & CHOICE OF DRINK (EVENTS ARE DEPENDENT)

SETTING A MULTIPURPOSE TABLE

	TEA	COFFEE	CHOCOLATE	TOTAL
MALE	57 2.356	26 2.013	11 0.355	94
FEMALE	42 2.089	47 1.785	17 0.314	106
TOTAL	99	73	28	200

$O_i$  = ACTUAL DATA - OBSERVED FREQUENCIES  
 $E_i$  = EXPECTED FREQUENCIES  
 $E_i^2$  = CONTRIBUTIONS,  $\frac{(O_i - E_i)^2}{E_i}$

SUMMARIZING THE LIST OF THE CONTRIBUTIONS

- DEGREES OF FREEDOM  $\bar{v} = (2-1)(2-1) = (2-1)(2-1) = 1 \times 2 = 2$
- CRITICAL VALUE  $\chi^2_{2}(5\%) = 5.991$
- $\sum \frac{(O_i - E_i)^2}{E_i} = 8.912$

$8.912 > 5.991$  THERE IS SOME EVIDENCE OF ASSOCIATION BETWEEN GENDER & CHOICE OF DRINK (DEPENDENT EVENTS)  
 SUFFICIENT EVIDENCE TO REJECT  $H_0$

## Question 4 (\*\*)

The table below summarizes the response of the University of Cambridge to 200 prospective mathematics applicants, originating from different type of English schools.

	State School	Grammar School	Private School
Offer	13	15	8
No Offer	76	67	21

Use a  $\chi^2$  test, at the 10% level of significance, to investigate whether there is any association between the type of school the applicant attends and the response of the University of Cambridge.

☐ , no association,  $2.505 < 4.605$

$H_0$ : THERE IS NO ASSOCIATION BETWEEN THE TYPE OF SCHOOL AN APPLICANT ATTENDS & THE UNIVERSITY'S RESPONSE (INDEPENDENCE)  
 $H_1$ : THERE IS ASSOCIATION BETWEEN THE TYPE OF SCHOOL AN APPLICANT ATTENDS & THE UNIVERSITY'S RESPONSE (DEPENDENCE)

SETTING UP A MULTIPURPOSE TABLE

	STATE SCHOOL	GRAMMAR SCHOOL	PRIVATE SCHOOL	TOTAL
OFFER	13 0.069	15 0.075	8 0.041	36
NO OFFER	76 0.425	67 0.345	21 0.108	164
TOTAL	89	82	29	200

$\text{O} = \text{ACTUAL DATA} = \text{OBSERVED FREQUENCIES}$   
 $\text{E} = \text{EXPECTED FREQUENCIES (E)}, \text{IF INDEPENDENT}$   
 $\text{O} - \text{E} = \text{CONTINGENCY } \frac{(O - E)^2}{E}$

SUMMARY OF THE TEST OF THE ASSUMPTIONS

- INDEGREE OF FREEDOM  $D = (r-1)(c-1) = (2-1)(3-1) = 1 \times 2 = 2$
- $\chi^2_{(0.1)} = 4.605$  ← CRITICAL VALUE
- $\sum \frac{(O - E)^2}{E} = 2.505$

As  $2.505 < 4.605$  THERE IS NO EVIDENCE OF ASSOCIATION BETWEEN THE TYPE OF SCHOOL AN APPLICANT ATTENDS, AND THE UNIVERSITY'S RESPONSE (INDEPENDENCE)

THERE IS NO SUFFICIENT EVIDENCE TO REJECT  $H_0$

**Question 5** (\*\*)

It is claimed that a new drug is effective in the prevention of sea sickness.

A large number of people that went on boat cruises were surveyed, and the results for a random sample of 100 individuals are summarized in the table below.

	Sickness	No Sickness
Drug Taken	25	50
No Drug Taken	15	10

Use a  $\chi^2$  test at the 5% level of significance to investigate whether there is evidence to support the claim made.

*You may not use a Yates correction in this question.*

☐ , claim justified,  $5.555 > 3.841$

$H_0$  : THERE IS NO ASSOCIATION BETWEEN THE EVENT OF TAKING THE DRUG & THE PREVENTION OF SEA-SICKNESS (INDEPENDENCE)  
 $H_1$  : THERE IS ASSOCIATION BETWEEN THE EVENT OF TAKING THE DRUG & THE PREVENTION OF SEA-SICKNESS (DEPENDENCE)

CONSTRUCTING A MULTIPURPOSE TABLE

	NO SICKNESS	NO SICKNESS	TOTAL
DRUG TAKEN	25 (31) 25	50 (49) 50	75
NO DRUG TAKEN	15 (10) 15	10 (15) 10	25
TOTAL	40 (41) 40	60 (64) 60	100

$O_i$  = ACTUAL DATA — OBSERVED FREQUENCIES ( $O_i$ )  
 $E_i$  = EXPECTED FREQUENCIES ( $E_i$ ), IF INDEPENDENT  
 $\frac{(O_i - E_i)^2}{E_i}$  = CONTRIBUTIONS  $\frac{(O_i - E_i)^2}{E_i}$

SUMMARISING ALL THE ABOVE

- DEGREES OF FREEDOM  $D.F. = (5-1)(2-1) = 2 \times 1 = 2$
- CRITICAL VALUE  $\chi^2_{(2)}(0.05) = 3.841$
- $\sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i} = 5.555$  (25)

As  $5.555 > 3.841$  THERE IS SOME EVIDENCE OF ASSOCIATION BETWEEN TAKING THE DRUG & THE PREVENTION OF SEA-SICKNESS  
 EVIDENCE TO SUPPORT THE CLAIM MADE  
 (SUFFICIENT EVIDENCE TO REJECT  $H_0$ )

**Question 6 (\*\*\*)**

The Dean of a faculty at a London University believes that the gender is independent of the class of the degree achieved.

A random sample of 240 male students and 80 female students were examined and the percentages for each gender are summarized in the table below.

	First Class	Second Upper	Second Lower or less
Male	22.5%	35%	42.5%
Female	20%	42.5%	37.5%

Use a  $\chi^2$  test, at the 10% level of significance, to investigate whether there is evidence to support the Dean's claim.

☐ , no association,  $1.451 < 4.605$

$H_0$ : THERE IS NO ASSOCIATION BETWEEN GENDER AND THE CLASS OF THE DEGREE ACHIEVED (INDEPENDENT EVENTS)  
 $H_1$ : THERE IS ASSOCIATION BETWEEN GENDER AND THE CLASS OF THE DEGREE ACHIEVED (DEPENDENT EVENTS)

• WRITE THE TABLE WITH ACTUAL DATA

	1st CLASS	2nd UPPER	2nd LOWER OR LESS	TOTAL
MALE	54 0.045	84 0.229	102 0.091	240
FEMALE	16 0.129	34 0.686	30 0.273	80
TOTAL	70	118	132	320

$\text{///}$  = ACTUAL DATA/OBSERVED FREQUENCY ( $O_i$ )  
 $\text{////}$  = EXPECTED FREQUENCY IF INDEPENDENT ( $E_i$ )  
 $\text{////}$  = CONTRIBUTION  $\frac{(O_i - E_i)^2}{E_i}$

• CALCULATING THE TEST OF THE INDEPENDENCE

$D = (C-1)(R-1) = (3-1)(2-1) = 2 \times 1 = 2$

$\sum_{i=1}^D \frac{(O_i - E_i)^2}{E_i} = 1.451$

$\chi^2_{(2)}(10\%) = 4.605$

• AS  $1.451 < 4.605$  THERE IS SIGNIFICANT EVIDENCE THAT THERE IS NO ASSOCIATION, SO DEAN IS JUSTIFIED - REJECT  $H_0$

## Question 7 (\*\*+)

The activities taken by the students of a school are summarized in the table below.

	Tennis	Rugby	Cricket	Badminton	Football
Boys	111	49	54	5	75
Girls	80	28	47	5	46

Use a  $\chi^2$  test, at the 10% level of significance, to investigate whether there is any association between the gender and the sport activity taken.

no association,  $2.536 < 6.251$

$H_0$ : There is no association between gender & choice of sport (independence)  
 $H_1$ : There is association between gender & choice of sport (not independent)

BADMINTON:  $E_1 = 59$   
 $E_2 = 64$   
 Total = 123

ANALYSE BADMINTON WITH TENNIS AS SIMILAR SPORTS AS NOT-HIGH EXPECTED FREQUENCIES LESS THAN 5

	TENNIS	BADMINTON	RUFGBY	CRICKET	FOOTBALL	TOTAL
BOYS	116	118.485	49	45.076	54	374
	0.001	0.001	0.001	0.001	0.001	0.001
GIRLS	85	80.515	28	31.924	47	226
	0.001	0.001	0.001	0.001	0.001	0.001
TOTAL	201	199	77	77	101	556

$O_i$  = OBSERVED  $O_i$  (ACTUAL DATA)  
 $E_i$  = EXPECTED  $E_i$  (NO INDEPENDENCE)  
 $\frac{(O_i - E_i)^2}{E_i}$  = CONTRIBUTION  $\frac{(O_i - E_i)^2}{E_i}$

- $\chi^2 = 3$
- $\chi^2_{0.10}(109) = 6.251$
- $\frac{3}{109} < \frac{6.251}{109}$

As  $2.536 < 6.251$  IT IMPLIES THAT THERE IS NO ASSOCIATION BETWEEN GENDER AND CHOICE OF SPORT (REJECT  $H_0$ )



**Question 8** (\*\*+)

A new car dealership wants to investigate whether there is an association between the type of engine of car they sell, and the claims made against the warranty they offer to their cars.

The table below summarizes 200 such claims made, classified by the engine type and by the age of the car.

	Claims in year 1	Claims in year 2 or 3	Claims after year 3
Petrol Engine	10	24	128
Diesel Engine	3	6	29

Use a  $\chi^2$  test, at the 10% level of significance, to investigate whether there is such association.

You need not use the Yates correction formula if you so wish in this question.

☐ , no association,  $1.092 < 2.705$

PROBLEM: HYPOTHESES AND FORM A TABLE OF ALL AVAILABLES

H<sub>0</sub>: THERE IS NO ASSOCIATION BETWEEN THE TYPE OF ENGINE AND THE OCCURRENCE OF MAKING A CLAIM (INDEPENDENT EVENTS)  
H<sub>1</sub>: THERE IS ASSOCIATION BETWEEN THE TYPE OF ENGINE AND THE OCCURRENCE OF MAKING A CLAIM (DEPENDENT EVENTS)

	CLAIMS IN YEAR 1	CLAIMS IN YEAR 2/3	CLAIMS IN YEAR 4+	TOTAL
PETROL ENGINE	10	24	128	162
DIESEL ENGINE	3	6	29	38
TOTAL	13	30	157	200

: OBSERVED VALUES (ACTUAL)  
 : EXPECTED VALUES (IF INDEPENDENT)  $\frac{\text{ROW TOTAL} \times \text{COLUMN TOTAL}}{\text{GRAND TOTAL}}$   
 : CONTRIBUTORS  $\frac{O-E}{E}$

LOOKING AT THE EXPECTED VALUES FOR DIESEL ENGINE CLAIMS IN YEAR 1

$\frac{13 \times 38}{200} = 2.47 < 5$

ANALYSING: LIST A 2ND ROW TO CLAIMS IN THE FIRST 3 YEARS

$D=1$  •  $\chi^2_{(10\%)} = 2.705$  •  $\sum \frac{(O-E)^2}{E} = 1.092$

AS  $1.092 < 2.705$  THERE IS EVIDENCE OF INDEPENDENCE, I.E. THERE IS NO ASSOCIATION BETWEEN ENGINE TYPE & OCCURRENCE OF CLAIM - SUFFICIENT EVIDENCE TO REJECT H<sub>0</sub>

**Question 9 (\*\*+)**

A random sample of 100 pupils from 4 local schools is classified by how many grade A/A\* GCSEs were achieved last year.

	0 – 2	3 – 5	6 +
School A	4	15	6
School B	1	17	7
School C	6	15	4
School D	6	12	7

Investigate whether there is any association between the number of grade A/A\* GCSEs achieved by students and the local school attended.

Use a  $\chi^2$  test, at the 10% level of significance.

no association,  $1.316 < 6.251$

$H_0$ : THERE IS NO ASSOCIATION BETWEEN TOP GRADES OF THESE SCHOOLS  
 $H_1$ : THERE IS ASSOCIATION BETWEEN "TOP GRADES" & "THESE SCHOOLS"

THE EXPECTED VALUES FOR SCHOOL A & SCHOOL B, E.g.  
 0-2 ARE BOTH 4.25, WHICH IS LESS THAN 5  
 THE "EASIEST" WAY TO COMBINE IS BY  
 AMALGAMATING THE FIRST TWO COLUMNS

	0-5	6+	TOTAL
A	19	6	25
B	18	7	25
C	21	4	25
D	18	7	25
TOTAL	76	24	100

$O_i$  = OBSERVED DATA  
 $E_i$  = EXPECTED IF HOMOGENEOUS  
 $\frac{(O_i - E_i)^2}{E_i}$  = CONTRIBUTIONS

$\chi^2 = (4-1) \times (2-1) = 3$   
 $\sum_{i=1}^4 \frac{(O_i - E_i)^2}{E_i} = \frac{25}{19} = 1.316$   
 $\chi^2_{(3)}(10\%) = 6.251$

AS  $1.316 < 6.251$  IT APPEARS  
 THAT THERE IS NO ASSOCIATION  
 BETWEEN TOP GRADES & THESE  
 4 SCHOOLS  
 (EXACT  $H_0$ )

**Question 10** (\*\*+)

Two groups of patients took part in a clinical trial for a new drug for a certain medical condition. One of the two groups was given the drug whilst the other group was given a placebo, a “fake” drug that has no physical effect in the medical condition.

The results are summarized in the table below.

	Placebo	Drug
Condition Improved	16	37
Condition Not Improved	43	24

Use a  $\chi^2$  test at the 5% level of significance to investigate whether there is any association between the type of drug patient were given and the improvement or not in their condition.

association,  $12.353 > 3.841$

$H_0$ : There is no association between drug given & improvement  
 $H_1$ : There is association between drug given & improvement

	PLACEBO	DRUG	TOTAL
IMPROVED	16 $\frac{3.586}{26.06}$	37 $\frac{3.39}{26.94}$	53
NOT IMPROVED	43 $\frac{2.773}{30.94}$	24 $\frac{2.683}{34.06}$	67
TOTAL	59	61	120

$O_{ij}$  = OBSERVED  $O_{ij}$   
 $E_{ij}$  = EXPECTED  $E_{ij}$   
 $\frac{(O_{ij} - E_{ij})^2}{E_{ij}}$  = YATES CORRECTION

- $\hat{p} = 1$
- $\chi^2_{(5\%)} = 3.841$
- $\sum_{i=1}^n \frac{(O_{ij} - E_{ij})^2}{E_{ij}} = 12.353$

As  $12.353 > 3.841$  there is evidence of association between the type of drug given and improvement (reject  $H_0$ )

**Question 11 (\*\*+)**

Research is carried out into the people's perception about their own bodyweight.

Subjects are being asked whether they think that they consider themselves overweight, underweight or at an ideal weight and the results are summarized in the table below.

	Underweight	Ideal Weight	Overweight
Male	27	29	40
Female	21	37	46

Investigate, using a  $\chi^2$  test, at the 10% level of significance, whether there is evidence that people's perception about their own bodyweight is independent of gender.

, no association,  $1.822 < 4.605$

FORMAL HYPOTHESES

$H_0$ : THERE IS NO ASSOCIATION BETWEEN PEOPLE'S PERCEPTION ABOUT THEIR OWN BODYWEIGHT AND GENDER — INDEPENDENT EVENTS

$H_1$ : THERE IS ASSOCIATION BETWEEN PEOPLE'S PERCEPTION ABOUT THEIR OWN BODYWEIGHT AND GENDER — NOT INDEPENDENT EVENTS

FORM A TABLE OF ACTUAL/OBSERVED FREQUENCIES AND CONTRIBUTIONS

	UNDERWEIGHT	IDEAL	OVERWEIGHT	TOTAL
MALE	27 23.04 0.681	29 31.68 0.227	40 41.28 0.040	96
FEMALE	21 34.56 0.628	37 34.56 0.209	46 44.72 1.037	104
TOTAL	48	66	86	200

OBSERVED FREQUENCY (ACTUAL DATA)  $O_i$   
 EXPECTED FREQUENCY (IF INDEPENDENT)  $E_i$   
 CONTRIBUTION  $\frac{(O_i - E_i)^2}{E_i}$

SUMMARYING INFORMATION

$\chi^2 = 2$        $\chi^2_{(10\%)} = 4.605$        $\frac{\sum (O_i - E_i)^2}{E_i} = 1.822$

As  $1.822 < 4.605$  THERE IS SIGNIFICANT EVIDENCE THAT THERE IS NO ASSOCIATION IE THE EVENTS ARE INDEPENDENT — SUFFICIENT EVIDENCE TO REJECT  $H_0$

## Question 12 (\*\*+)

Two schools, A and B, entered their A Level mathematics for a Mathematics Competition of which three different results were possible.

These results are summarized in the table below.

	Credit	Pass	Fail
School A	51	10	19
School B	39	10	21

Use a  $\chi^2$  test, at the 5% level of significance, to investigate whether there is evidence that the proportions of these results are different between the two schools.

no association,  $1.032 < 5.991$

	Credit	Pass	Fail	TOTAL
A	51 $\frac{51-46}{46} = 0.1087$	10 $\frac{10-20}{20} = -0.5$	19 $\frac{19-25}{25} = -0.2$	80
B	39 $\frac{39-46}{46} = -0.1522$	10 $\frac{10-20}{20} = -0.5$	21 $\frac{21-25}{25} = -0.16$	70
TOTAL	90	20	40	150

$H_0$ : THERE IS NO ASSOCIATION BETWEEN THE SCHOOLS AND THE STUDENTS' PERFORMANCE (RANDOMISED DATA)  
 $H_1$ : THERE IS ASSOCIATION BETWEEN THE SCHOOLS AND THE STUDENTS' PERFORMANCE (NOT RANDOMISED EVENTS)

$O_i$ : OBSERVED VALUES (ACTUAL DATA)  
 $E_i$ : EXPECTED VALUES (IF HYPOTHESIS)  
 $\frac{(O_i - E_i)^2}{E_i}$ : CONTRIBUTIONS

THIS IS  $\chi^2 = 2 \times (3-1)(2-1)$   
 $\sum \frac{(O_i - E_i)^2}{E_i} = 1.0322$   
 $\chi^2_{2, 0.05} = 5.991$

AS  $1.0322 < 5.991$  THERE IS EVIDENCE OF INDEPENDENCE BETWEEN THE PERFORMANCES OF THE TWO SCHOOLS (NO ASSOCIATION) REJECT  $H_0$

## Question 13 (\*\*+)

A random sample of 250 employees of a certain town were classified by their level of education and their eventual average annual earnings.

	Non Graduates	Graduates	Post Graduates
Up to £10000	17	6	3
£10001 to £25000	97	16	3
£25001 to £40000	42	21	8
Over £40000	24	10	6

Use the sample to investigate whether there is any association between level of education and the eventual average annual earnings of the employees.

Use a  $\chi^2$  test, at the 1% level of significance.

, association,  $18.861 > 11.345$

SETTING: Suitable hypotheses

- $H_0$ : There is no association between the education level and the eventual average earnings (independence)
- $H_a$ : There is association between the education level and the eventual average earnings (not independent)

EDUCATION LEVEL

	Non Graduates	Graduates	Post Graduates	TOTAL
Up to £10000	17	6	3	26
£10001 to £25000	97	16	3	116
£25001 to £40000	42	21	8	71
Over £40000	24	10	6	40
TOTAL	180	53	17	250

EARLY LOOKING AT SOME OF THE FREQUENCIES, WE SUSPECT THAT THE EXPECTED FREQUENCIES MIGHT FALL BELOW 5

- check "Post Graduates under £10000":  $\frac{26 \times 17}{250} = 1.84 < 5$
- combine the last two columns of the table

COMPUT: EXPECTED FREQUENCIES & CONTRIBUTIONS

- : observed frequencies (actual data),  $O_i$
- : expected frequencies for independence,  $E_i$
- : contributions,  $\frac{(O_i - E_i)^2}{E_i}$

SUMMARIZING ALL RESULTS

$\chi^2 = 18.861$

$\chi^2_{0.01}(3) = 11.345$

$\sum \frac{(O_i - E_i)^2}{E_i} = 18.861$

As  $18.861 > 11.345$  there is significant evidence of association (dependence) between the level of education and the eventual average annual earnings.

There is sufficient evidence to reject  $H_0$ .

**Question 14** (\*\*\*)

An investigation was carried out to determine the effectiveness of four different blood pressure lowering medications.

Each of the 100 patients who took part in the investigation was given one of the four available medications  $A$ ,  $B$ ,  $C$  or  $D$ .

- 10 of the 17 patients that were given medication  $A$  had a positive response.
- 16 of the 26 patients that were given medication  $B$  had a positive response.
- 15 of the 28 patients that were given medication  $C$  had a positive response.
- 11 of the 29 patients that were given medication  $D$  had a positive response.

The following claims are made.

## a) Claim 1

Each patient was randomly given one of the four medications.

## b) Claim 2

The patient's response is independent of the medication that was given.

Test each of these claims at the 10% level of significance.

claim 1 justified,  $3.6 < 6.251$

claim 2 justified,  $3.592 < 6.251$

③  $H_0$ : DATA COULD BE MODELLED BY A UNIFORM DISCRETE DISTRIBUTION  
 $H_1$ : DATA COULD NOT BE MODELLED BY A UNIFORM DISCRETE DISTRIBUTION

	A	B	C	D	
(E)	25	26	28	29	
(O)	17	26	28	29	
$(O-E)^2/E$	64/25	1/26	0/28	16/29	
$\sum$	2.56	0.038	0	0.552	3.15

$\chi^2_{(3)}(10\%) = 6.251$   
 $\chi^2_{(3)} = 3.15 < 6.251$   
 THERE IS SUFFICIENT EVIDENCE THAT DATA COULD FIT A UNIFORM DISCRETE DISTRIBUTION. (REJECT  $H_0$ )  
 $\therefore$  CLAIM 1 IS JUSTIFIED

④

	A	B	C	D	TOTAL
INPUT	10	16	15	11	52
NOT INPUT	7	10	13	18	48
TOTAL	17	26	28	29	100

$\chi^2_{(3)}(10\%) = 6.251$   
 $\chi^2_{(3)} = 3.592 < 6.251$   
 THERE IS SUFFICIENT EVIDENCE THAT DATA COULD FIT A UNIFORM DISCRETE DISTRIBUTION. (REJECT  $H_0$ )  
 $\therefore$  CLAIM 2 IS JUSTIFIED

⑤

	A	B	C	D	TOTAL
INPUT	10	16	15	11	52
NOT INPUT	7	10	13	18	48
TOTAL	17	26	28	29	100

$\chi^2_{(3)}(10\%) = 6.251$   
 $\chi^2_{(3)} = 3.592 < 6.251$   
 THERE IS SUFFICIENT EVIDENCE THAT DATA COULD FIT A UNIFORM DISCRETE DISTRIBUTION. (REJECT  $H_0$ )  
 $\therefore$  CLAIM 2 IS JUSTIFIED