

Created by T. Madas

INTEGRATION

BY REVERSE CHAIN RULE

(WITHOUT ANSWERS)

Created by T. Madas

Question 1

Carry out each of the following integrations.

1. $\int 3x(x^2 - 1)^4 dx$

2. $\int x^2(1 - 4x^3)^{-\frac{1}{2}} dx$

3. $\int 4\sin^3 x \cos x dx$

4. $\int \sin x \cos^2 x dx$

5. $\int \frac{10x}{\sqrt{x^2 - 7}} dx$

6. $\int 6xe^{x^2} dx$

7. $\int \tan^4 x \sec^2 x dx$

8. $\int \sec^4 x \tan x dx$

9. $\int e^{\sin 2x} \cos 2x dx$

10. $\int \frac{\ln x}{x} dx$

11. $\int \sqrt{\cos x \sin 2x} dx$

12. $\int \frac{1}{\sqrt{x^{\frac{3}{2}} + 5x}} dx$

Question 2

Carry out each of the following integrations.

1.
$$\int \frac{x^3}{x^4 + 2} dx$$

2.
$$\int \frac{x^2}{4 - x^3} dx$$

3.
$$\int \frac{4x}{x^2 - 1} dx$$

4.
$$\int \frac{3x^2}{1 + x^3} dx$$

5.
$$\int \frac{3e^{2x}}{e^{2x} - 1} dx$$

6.
$$\int \frac{4\sec^2 x}{\tan x} dx$$

7.
$$\int \frac{x}{9x^2 + 1} dx$$

8.
$$\int \frac{\operatorname{cosec}^2 x}{1 + \cot x} dx$$

9.
$$\int \frac{4x}{x^2 - 10} dx$$

10.
$$\int \frac{2^x}{2^x + 1} dx$$

Question 3

Carry out each of the following integrations.

1. $\int \frac{x}{x^2 - 9} dx$

2. $\int \frac{10x}{x^2 - 9} dx$

3. $\int \frac{3x}{4 - 2x^2} dx$

4. $\int \frac{x^2}{x^3 + 1} dx$

5. $\int \frac{2x + 6}{x^2 + 6x + 1} dx$

6. $\int \frac{4e^{3x}}{1 - e^{3x}} dx$

7. $\int \frac{3^x}{3^x + 1} dx$

8. $\int \frac{5^{2x}}{5^{2x} + 3} dx$

9. $\int \frac{x - 2}{x^2 - 4x - 2} dx$

10. $\int \frac{\sin x - \cos x}{\sin x + \cos x} dx$

Question 4

Carry out each of the following integrations.

1. $\int \frac{x}{(x^2-1)^3} dx$

2. $\int \cos x \sin x dx$

3. $\int \frac{4x}{\sqrt{1-2x^2}} dx$

4. $\int \sec^2 x (1 + \tan^2 x) dx$

5. $\int \sec^2 x (1 + \tan x) dx$

6. $\int \sec x \tan x \sqrt{\sec x + 1} dx$

7. $\int \tan^2 x \sec^2 x dx$

8. $\int e^{\sin x} \cos x dx$

9. $\int \sqrt{\sin x \cos^2 x} dx$

10. $\int (2x+1)(x^2+x+1) dx$

Question 5

Carry out each of the following integrations.

1.
$$\int (2x+1) \sin(x^2+x+1) dx$$

2.
$$\int (x+1) \cos(x^2+2x+1) dx$$

3.
$$\int \frac{1}{x(1+\ln x)^3} dx$$

4.
$$\int 4 - \cos^4 x \sin x dx$$

5.
$$\int \frac{\cos x}{\sin^3 x} dx$$

6.
$$\int \frac{\sqrt{1+2 \tan x}}{\cos^2 x} dx$$

7.
$$\int \frac{\cos x}{\sqrt{\sin x}} dx$$

8.
$$\int \frac{1}{x \ln x} dx$$

9.
$$\int \frac{1}{\cos^2 x \tan^4 x} dx$$

10.
$$\int \sin^3 2x \cos 2x dx$$

Question 6

Carry out each of the following integrations.

1.
$$\int \frac{\cos(\ln x)}{x} dx$$

2.
$$\int \frac{3x}{\sqrt{4-2x^2}} dx$$

3.
$$\int \frac{\sin x}{\cos^4 x} dx$$

4.
$$\int \cos x \sin^3 x dx$$

5.
$$\int \frac{\sin^2 x}{\cos^4 x} dx$$

6.
$$\int e^x \sin(e^x) dx$$

7.
$$\int \sin 2x \cos^4 2x dx$$

8.
$$\int 3x^2 (4-2x^3)^{\frac{3}{2}} dx$$

9.
$$\int \frac{x+1}{\sqrt[3]{x^2+2x+3}} dx$$

10.
$$\int \sin 2x \cos 2x dx$$

Question 7

Carry out each of the following integrations.

1.
$$\int \frac{(\ln x)^2}{x} dx$$

2.
$$\int (x+1)(x^2+2x+1)^4 dx$$

3.
$$\int \sin x \cos^4 x dx$$

4.
$$\int \sec^3 x \tan x dx$$

5.
$$\int x(3+x^2)^4 dx$$

6.
$$\int \frac{\cos x}{\sqrt{\sin^3 x}} dx$$

7.
$$\int \cos x \sqrt{\sin x} dx$$

8.
$$\int \frac{\sec^2 x}{(1+\tan x)^3} dx$$

9.
$$\int \frac{\sin x \cos x}{\sqrt{\cos 2x+1}} dx$$

10.
$$\int \frac{\ln x^2}{x} dx$$

Question 8

Carry out each of the following integrations.

1.
$$\int 3x^2(4-2x^3)^{\frac{3}{2}} dx$$

2.
$$\int \frac{e^{\sqrt{x}}}{\sqrt{x}} dx$$

3.
$$\int \frac{\sqrt{\sqrt{x}+1}}{\sqrt{x}} dx$$

4.
$$\int \frac{x}{\sqrt{x^2+1}} dx$$

5.
$$\int \frac{1}{\sqrt{x} \cos^2 \sqrt{x}} dx$$

6.
$$\int \frac{x}{\sqrt{x^2+1}} dx$$

7.
$$\int \frac{1}{\sqrt{x}\sqrt{\sqrt{x}+1}} dx$$

8.
$$\int \frac{\sin x}{\cos^5 x} dx$$

9.
$$\int x\sqrt{1-x^2} dx$$

10.
$$\int \sqrt{\frac{2\sqrt{x}+3}{4x}} dx$$

Question 9

Carry out each of the following integrations.

1. $\int_0^2 \frac{2x}{\sqrt{x^2+4}} dx = 4(\sqrt{2}-1)$

2. $\int_0^{36} \frac{1}{\sqrt{x}(\sqrt{x}+2)} dx = \ln 16$

3. $\int_0^3 \frac{x}{x^2+9} dx = \frac{1}{2} \ln 2$