

1. a) $6(1-x^2)^5 \times (-2x)$

← ^{der}
M1 M1

b) $x^3 \times 3\cos 3x + 3x^2 \times \sin 3x$

B1 (sensible attempt at product rule)
M1 M1

c) $\frac{(x^3+2) \times 5 - 5x(3x^2)}{(x^3+2)^2}$

M3 ~~der~~ on ~~der~~ attempt on quotient rule

2. Use $\sec'' 2x = \frac{1}{\cos'' 2x}$

B1

$\cos 2x = 1 - 2\sin^2 x$

B1

$1 - 2\left(\frac{3}{5}\right)^2$

M1

$1 - \frac{18}{25}$ & successful conclusion

A1

3. $x^2 - 2x - 4 = 4$

B1

$x^2 - 2x - 4 = -4$

B1

$(x-4)(x+2)$ OR $x(x-2)$

M1

$x = -2, 4, 0, 2$

A2

4. a) $f(0.7) = -0.13265$
 $f(0.8) = 0.04743$ } BOTH ATTEMPTED M1

CHANGE OF SIGN (AND CONTINUITY) IMPLIES ROOT... E1

b) $x = \frac{1}{4} + \frac{3}{4} \sin x$ OR $x_{n+1} = \frac{1}{4} + \frac{3}{4} \sin x_n$
 OR $A = \frac{1}{4}, B = \frac{3}{4}$ M1

$x_2 = 0.76123$ -

$x_3 = 0.76739$ -

$x_4 = 0.77068$ -

$x_5 = 0.77247$ -

A3 -1 eoo

c) ATTEMPTS $f(0.7745)$ OR $f(0.7755)$ OR "ITERATE" M1

0.000076 OR 0.0017804 SEEN A1

0.7745 < x < 0.7755 + CONCLUSION E1

5. a) ≈ 205 A1

b) 400 A1

d) $1000 = 400 e^{\frac{1}{12}(t-12)}$ M1

$\frac{5}{2} = e^{\frac{1}{12}(t-12)}$ M1

$\ln \frac{5}{2} = \frac{1}{12}(t-12)$ M1

$t = 8 + 12 \ln \frac{5}{2}$ OR 18.995... A1
 OR 19

6. REFLECTION IN THE x AXIS SEEN OR IMPUND, MUST TOUCH x AXIS B1
 TRANSLATION "LEFT" SEEN OR IMPUND B1
 $(-7,0)$ & $(-1,0)$ (BOTH) A1
 $(-5,0)$ A1

7. $2(2\cos\theta - 1) = 4\cos\theta - 3$ M1
 $4\cos^2\theta - 4\cos\theta + 1 = 0$ O.E. M1
 $(2\cos\theta - 1)^2 = 0$ O.E. M1
 $\cos\theta = \frac{1}{2}$ A1
 $\theta = 60$ A1
 $\theta = 300$ A1

8. a) $\frac{2(2x-1)-6}{(x-2)(2x-1)}$ M1
 $\frac{4x-8}{(x-2)(2x-1)}$ M1
 $\frac{4(x-2)}{(x-2)(2x-1)}$ M1
 CANCELS OR SIMPLIFY ANSWER A1 \uparrow dte

b) $x = \frac{1}{2}$ c.a.o B1

c) $0 < f(x) < 4$ M1 M1

d) $2xy - y = 4$ OR $2x - 1 = \frac{4}{y}$ M1

$x = \frac{y+4}{2y}$ OR $x = \frac{1}{2}\left(\frac{4}{y} + 1\right)$ O.E. M1

$f(x) = \frac{y+4}{2y}$ OR $f(x) = \frac{2}{y} + \frac{1}{2}$ O.E. A1

e) $0 < x < 4$ A1 ~~at~~ (b) $f(x) > 1$ A1

$$9. a) \frac{dy}{dx} = \frac{(4x-k) \times 4 - (4x+k) \times 4}{(4x-k)^2}$$

M3 b/c on correct quotient rule structure

$$\frac{16x - 4k - 16x - 4k}{(4x-k)^2}$$

M1

$$= \frac{-8k}{(4x-k)^2} \text{ or SIMILAR}$$

-11

$$b) \frac{-8k}{(12-k)^2} = \frac{8}{27}$$

M1

SIMPLIFIED TO "NON DENOMINATOR EXPRESSION" (GUESS ATTEMPT) M1

$$k^2 - 51k + 144 = 0$$

A1

$$(k-48)(k-3) = 0$$

M1

$$k = \begin{matrix} 3 \\ 48 \end{matrix} \text{ BOTH}$$

A1

$$10. a) \sin 2x \cos x + \cos 2x \sin x$$

M1

$$(2 \sin x \cos x) \cos x + (1 - 2 \sin^2 x) \sin x$$

M2

$$2 \sin x \cos^2 x + \sin x - 2 \sin^3 x$$

M1

$$2 \sin x (1 - \sin^2 x) + \sin x - 2 \sin^3 x$$

M1

$$2 \sin x - 2 \sin^3 x + \sin x - 2 \sin^3 x + \sin x$$

-A1

$$b) 3 \cos 3x = 3 \cos x - 12 \sin^2 x \cos x$$

M2

USE OF $1 - \cos^2 x$ INTO

M1

$$\begin{aligned} (3 \cos 3x &= 3 \cos x - 12 \cos x + 12 \cos^3 x) \\ \text{or } (\cos 3x &= \cos x - 4 \cos x + 4 \cos^3 x) \end{aligned}$$

M1

$$\cos 3x = 4 \cos^3 x - 3 \cos x$$

A1