

1.

SIGHT OF $\frac{5\pi}{6}$ BI

(USE OF STANDARD TRIGONOMETRY ON) MI
($\triangle OBC$, OR SINE RULE)

$(|OC| = \frac{6}{5}\sqrt{3} \text{ o.e.})$ AI
 $(|BC| = \frac{6}{5} \text{ o.e.})$

AREA OF $\triangle OBC$ AS $\frac{1}{2} \times \frac{6}{5}\sqrt{3} \times \frac{6}{5}$ OR $\frac{1}{2} \times \frac{6}{5}\sqrt{3} \times \sin\frac{5\pi}{6}$ MI

AREA OF SECTOR = $\frac{1}{2} \times 2.4^2 \times \frac{5\pi}{6}$ MI

(AREA OF $\triangle OBC = \frac{18}{25}\sqrt{3}$ OR 1.247...) AI
OR
AREA OF SECTOR = $\frac{12\pi}{5}$ OR 7.5398...)

A.W.P.T 8-79 c.a.o AI

2.

$(y =) \frac{1}{4}x + x^{-1}$ o.e. BI

$\frac{dy}{dx} = \frac{1}{4} - x^2$ MI

" $\frac{1}{4} - x^2$ " > 0 MI

$x^2 > 4$ AI



MI SIGHT OF BOTH -2 & 2

MI DIAGRAM OR EQUIVALENT.

$x < -2$ OR $x > 2$

AI \nearrow dep

DO NOT ACCEPT \leq \geq
DO NOT ACCEPT $2 < x < -2$
ACCEPT "AND" INSTEAD OF "OR"

3. $a + ar = 240$ OR $\frac{a(r^2-1)}{r-1} = 240$ M1

$a + ar^2 = 200$ M1

SUBSTITUTION OR DIVISION OF EQUATIONS M1

$6r^2 - 5r + 1$ A1

$(3r-1)(2r-1)$ M1

$r = \begin{cases} \frac{1}{2} \\ \frac{1}{3} \end{cases}$ BOTH

$a = \begin{cases} 160 \\ 180 \end{cases}$ BOTH

$\frac{160}{1-\frac{1}{2}}$ OR $\frac{180}{1-\frac{1}{3}}$

M1

320 & 270 (BOTH)

A1

4. $8 \left(\frac{\sin x}{\cos x} \right)^2 \sin x = \cos x$ OR $\frac{8 \sin^2 x}{\cos^2 x} \sin x = \cos x$ M1

$8 \sin^3 x = \cos^3 x$ M1

$8 \tan^3 x = 1$ OR $\tan^3 x = \frac{1}{8}$ M1

$\tan x = \frac{1}{2}$ A1

A.W.R.T 0.46° & 3.61° c.a.o A1 A1

ALTERNATIVE FOR THE FIRST 3 MARKS

M1 DIVIDES EQUATION BY $\cos x$ TO GET $\frac{8 \tan^3 x \sin x}{\cos x} = 1$

M1 USES $\frac{\sin x}{\cos x} = \tan x$

M1 THEN STATES $8 \tan^3 x = 1$

5. a) $3^3 - 2 \times 3^2 - 3 - 6$ M1
 OBTAINS ZERO & CONCLUDES A1

b) $(x-3)(x^2 + Ax + B)$ M1
 $(x-3)(x^2 + x + 2)$ A1

c) $\left(\frac{dy}{dx}\right) = 12x^3 - 24x^2 - 72x + 240$ M1

" $12x^3 - 24x^2 - 72x + 240 = 0$ " M1

$x^3 - 2x^2 - x - 6 = 0$ A1

ATTEMPTS DISCRIMINANT ON $x^2 + x + 2$ M1

OBTAINS ⁽⁻⁾ NEGATIVE & STATES ONLY SOLUTION OR STATIONARY POINT IS AT $x=3$ A1

OBTAINS y CO-ORD OF -3 A1

$\frac{d^2y}{dx^2} = 36x^2 - 48x - 12$ M1

USES $\frac{d^2y}{dx^2}$ CORRECTLY OBTAINS ⁽¹⁶⁸⁾ POSITIVE & STATES MINIMUM A1

6. $\left[\begin{matrix} (13) \\ (5) \\ \text{OR } 8 \end{matrix} \right] \left[\begin{matrix} 5 \\ \left(\frac{9}{2x}\right) \left(-\frac{2x^2}{3}\right) \end{matrix} \right]$ M1 M1

92664 cap A1

7.

$$\begin{pmatrix} 19000 = A \times 10^{3k} \\ \text{(OR)} \\ 38000 = A \times 10^{6k} \end{pmatrix} \quad \begin{matrix} \text{M1} \\ \text{M1} \end{matrix}$$

SUBSTITUTES OR DIVIDES M1

$$10^{3k} = 2 \quad \text{o.e.} \quad \text{A1}$$

USES LOGS CORRECTLY M1

$$k = \frac{1}{3} \log 2 \quad \text{A.M.R.T.} \quad 0.10 \quad \text{A1}$$

$$A = 9500 \quad \text{A1}$$

8.

IMPLIES THAT CENTRE OF C_3 LIES ON $x=12$ M1

(SIGHT OF " $6+r$ " OR " $6-r$ " OR TRIANGLE
DRAWN WITH VERTICES AT CENTRE OF C_1 , CENTRE
OF C_3 & INTERSECTION OF C_1 & C_2) M1

$$"6^2 + (6-r)^2 = (6+r)^2" \quad \text{i.e. USE OF PYTHAGORAS} \quad \text{M1}$$

EXPANDS & SIMPLIFIES CORRECTLY M1

$$"r" = 1.5 \quad \text{o.e.} \quad \text{A1}$$

$$\boxed{(x-12)^2 + \left(y - \frac{3}{2}\right)^2} = \boxed{\frac{9}{4}} \quad \text{o.e.} \quad \text{A1} \quad \text{A1}$$

9. IMPLIES OR STATE $A(0,6)$ BI

$\left(\begin{array}{l} (2x-1)(x-6) \\ \text{OR} \\ B(\frac{1}{2},0) \quad C(6,0) \quad (\text{OR IMPLIES}) \end{array} \right)$ BI

$D(\frac{13}{2},6)$ (OR IMPLIES) BI

$\left(\begin{array}{l} \int_0^{\frac{1}{2}} 2x^2 - 13x + 6 \, dx \\ \text{OR} \\ \int_6^{\frac{13}{2}} 2x^2 - 13x + 6 \, dx \end{array} \right)$ MI
MI UNITI BOTT

$\cdot \frac{2}{3}x^3 - \frac{13}{2}x^2 + 6x$ MI

$\left(\begin{array}{l} \left[\frac{1}{12} - \frac{13}{8} + 3 \right] - [0] \\ \text{OR} \\ \left[\frac{2197}{12} - \frac{2197}{8} + 39 \right] - [144 - 234 + 36] \end{array} \right)$ MI

$\frac{35}{24}$ AI

SIGN OF 39 & 18 (BOTT) MI

FINAL ANSWER $\frac{469}{24}$ AI

10. a) SPACING OF 0.4 USED BI

$$\left(\begin{array}{cccccc} \frac{a}{2} & \frac{5}{12}a & \frac{5}{14}a & \frac{5}{16}a & \frac{5}{18}a & \frac{a}{4} \\ \frac{a}{2} & \frac{a}{2.4} & \frac{a}{2.8} & \frac{a}{3.2} & \frac{a}{3.6} & \frac{a}{4} \end{array} \right) \text{MI}$$

"THICKNESS $\left[\frac{\text{FIRST} + \text{LAST} + 2 \times (\text{SUM OF THE REST})}{2} \right]$ " MI

$$\frac{1753}{2520}a = 701.2 \quad \text{OR} \quad 0.6956...a = 701.2 \quad \text{MI}$$

$$a = 1008 \text{ c.a.o} \quad \text{AI}$$

b) IMPULS OR STATES "AREA STRETCHES VERTICALLY" BY SCALE FACTOR OF 5 BI

IMPULS OR STATES "AREA STRETCHES HORIZONTALLY" BY SCALE FACTOR $\frac{1}{2}$ BI

STATES 1753 AI

(THIS MARK CAN ONLY BE ACHIEVED IF AT LEAST ONE OF THE PREVIOUS BI MARKS OF PART (b) HAS BEEN AWARDED)