

1. a) ATTEMPT $P(x)$ e.g. $16 - 4x + 4x - 12$ M1

OBTAINS ZERO & CONCLUDES A1

b) $(x-2)(2x^2-7x+6)$ M1

$(x-2)(x-2)(2x-3)$ A1

c) -112 c.a.o. A1

d) $a = -15$ A1

$b = 50$ A1

$c = -112$ A1

2 a) $(4, 2)$ B1, B1

$\sqrt{20}$ OR $2\sqrt{5}$ B1

b) SIGHT OF $y^2 = 4y$ OR $x^2 = 8x$ o.e. M1

$(8, 0)$ & $(0, 4)$ A1 A1

c)

- CIRCLE THROUGH O
- CHORD IN 1st QUADRANT
- $(8, 0)$ $(0, 4)$ MARKED

 G2 + e.e.o.o.

d) $\boxed{AOB = 90^\circ \Rightarrow AB \text{ IS A DIAMETER}}$

MUST BE SEEN OR "AU" IMPLIED

A1

so $4\sqrt{5}$ OR $\sqrt{20}$

(ALLOW $\sqrt{20}$ INCORRECTLY IF REASON IS CORRECT)

3.

$$\log_2 \left(\frac{2z+1}{z} \right) \text{ OR } \log_2(4z) \quad M1$$

$$\frac{2z+1}{z} = 4 \quad \text{o.e.} \quad M1$$

$$z = \frac{1}{2} \quad \text{C.A.O.} \quad A1$$

4.

a) USE OF PYTHAGORAS M1

OBTAINS HEIGHT 24 M1

AREA = 168 A1

b1) COSINE RULE USE M1

ALL CORRECT TO ANSWER A1

$$b1) \left. \begin{array}{l} \text{OR } \sin \theta = \frac{7}{25} \\ \cos \theta = \frac{24}{25} \\ \tan \theta = \frac{7}{24} \end{array} \right\} \text{ ANY OF THESE o.e. M1}$$

$$\underline{2 \times 0.2837 \dots} = 0.568 \quad A1$$

(alb)

USE OF COSINE RULE M1

$$\cos \theta = \frac{527}{625} \approx 0.843 \dots \quad M1$$

$$\theta = 0.5675 \dots \quad A1$$

$$\frac{1}{2} \times 25 \times 25 \times \sin(0.5675 \dots) \quad M1$$

A.W.T 168 A1

$$c) \text{ AREA OF SEMICIRCLE} = \frac{1}{2} \times \pi \times 7^2 \quad \text{OR A.W.T 76.97 B1}$$

$$\text{ AREA OF SECTOR} = \frac{1}{2} \times 25^2 \times 0.5675 \dots \quad \text{OR A.W.T. 177 or 178}$$

$$\text{ FINAL ANSWER } 67.5 \pm 0.5 \quad A1$$

5. a) $\frac{k}{2k-5} = \frac{k-6}{k}$ o.e. BI

REARRANGES CORRECTLY & CONVINCINGLY TO ANSWER GIVEN MAI

b) FACTORIZES $(k-2)(k-15)$ OR SIGHT OF 2 & 15 MI

$-1, 2, -4$ OR $25, 15, 9$ SEEN BI

$$\frac{25}{1 - \frac{3}{5}}$$

MI "STRUCTURE"

MI ALL CORRECT

$$\frac{125}{2} \text{ c.a.o}$$

AI

(o.e)

c) $\frac{-1((-2)^{10} - 1)}{-2 - 1}$ o.e. e.g. $\frac{-1(1 - (-2)^{10})}{1 - (-2)}$ MI

341 c.a.o AI

6. a) $k^n + nk^{\frac{n-1}{2}} + \frac{1}{2}n(n-1)k^{\frac{n-2}{2}}x^2 + \frac{1}{6}n(n-1)(n-2)k^{\frac{n-3}{2}}x^3$ MI
MI

SETS COEFFICIENTS FIRST & DIVIDES OUT / DIVIDES
 $n(n-1)$ / $k^{\frac{n-2}{2}}$ MI MI

CONVICINGLY GETS THE ANSWER $n = 3k + 2$ AI

b) $\begin{pmatrix} 8 \\ 4 \end{pmatrix} 2^4 x^4$ MI

1120 c.a.o AI

7. a) $\frac{1}{2}x^2 \sin 60$ or $\frac{1}{4}x^2\sqrt{3}$ B1

$3xy + \left(\frac{1}{4}x^2\sqrt{3}\right) \times 2 = 54\sqrt{3}$ M1

$V = \left(\frac{1}{4}x^2\sqrt{3}\right) \times y$ M1

SUBS AN EXPRESSION FOR y M1

OBTAINS ANSWER WITH
CONVINCING A1

b) $\left(\frac{dv}{dx}\right) = \frac{27}{2} - \frac{3}{8}x^2$ M1

$\frac{27}{2} - \frac{3}{8}x^2 = 0$ M1

OBTAINS CORRECTLY $x=6$ A1

$\left(\frac{d^2v}{dx^2}\right) = -\frac{3}{4}x$ M1

SUBS $x=6$ INTO HERE " $\frac{d^2v}{dx^2}$ ", OBTAINS NEGATIVE M1
& STATES MAX

STATES $(V_{\max}) = 54$ A1

c) SUBS $x=6$ INTO HERE " $3xy + \frac{1}{4}x^2\sqrt{3} \times 2 = 54\sqrt{3}$ " M1

OBTAINS $y = 2\sqrt{3} \approx 3.46$ o.e. A1

8. a)

$$\begin{aligned} -3 &= P + Q \\ 5 &= P + Q \end{aligned} \quad \text{OR} \quad \text{MENTION OF TRANSFORMATIONS}$$

M1

$P=1$ A1 \rightarrow dep \nearrow ON A METHOD
 $Q=4$ A1 \rightarrow

b) $4 \cos 2\alpha + 1 = 0$ B1

$\cos 2\alpha = \frac{1}{4}$ M1

SIGHT OF $1.3181\dots$ B1 ($\pm 75.52\dots$)

OR SIGHT OF $4.681\dots$ B1 ($284.48\dots$)

A.W.R.T $0.66^\circ, 2.48^\circ, 3.80^\circ, 5.62^\circ, 69.4^\circ, 8.77^\circ$

-1 eeo A2
(IGNORE EXTENS)

(ALLOW WORKINGS IN DEGREES EXCEPT FINAL TWO ANSWER MARKS)

9.

ATTEMPTS TO FIND INTERSECTIONS WITH $y=8$ OR WITH $y=5$ M1

POINTS TOGETHER 1 & 3 OR (1,8) (3,8) MA1

POINTS TOGETHER 0 & 4 OR (0,5) (4,5) MA1

$\int 5 + 4x - x^2 dx$ LIMITS \int_0^1 OR \int_3^4 M1 M1

$5x + 2x^2 - \frac{1}{3}x^3$ M1

[.....] - [.....] THEN LIMITS M1

SIGHT OF $\frac{20}{3}, \frac{5}{3}, 5$ AND/OR 6

ADD/SUBTRACTED (AT LEAST TWO OF THESE SEEN) M1

FINAL ANSWER $\frac{28}{3}$ A1 c.a.o